Trees

Tree Processing

# Solving Tree Problems

#### Tree-Structured Data

### Solving Tree Problems

 $Implement \ \ \frac{bigs}{bigs}, \ which \ takes \ a \ Tree \ instance \ t \ containing \ integer \ labels. \ It \ returns \ the number of nodes in t whose labels are larger than any labels of their ancestor nodes.$ 

Recursive Accumulation

#### Solving Tree Problems

Implement bigs, which takes a Tree instance t containing integer labels. It returns the number of nodes in t whose labels are larger than any labels of their ancestor nodes.

```
def bigs(t):
    """Return the number of nodes in t that are larger than all their ancestors."""
  nonlocal n
                      __: __node.label > max_ancestors
     if a.label > x
                   Somehow increment the total count
     for b in a.branches
```

### How to Design Programs

From Problem Analysis to Data Definitions
Identify the information that must be represented and how it is represented in the chosen programming language. Formulate data definitions and illustrate them with examples.

Signature, Purpose Statement, Meader
State what kind of data the desired function consumes and produces. Formulate a concise answer to the question what the function computes. Define a stub that lives up to the signature.

Functional Examples Work through  $\underline{\text{examples}}$  that illustrate the function's purpose.

Function Template Translate the data definitions into an outline of the function.

Function Definition Fill in the gaps in the function template. Exploit the purpose statement and the  $\underline{\text{examples}}$ .

Testing
Articulate the <u>examples</u> as tests and ensure that the function passes all. Doing so discovers mistakes. Tests also supplement examples in that they help others read and understand the definition when the need arises—and it will arise for any serious program.

https://htdp.org/2018-01-06/Book/

# Designing a Function

```
Implement smalls, which takes a Tree instance t containing integer labels. It returns the non-leaf nodes in t whose labels are smaller than any labels of their descendant nodes.
```

```
non-tear nodes in t whose labels are smaller than any labels of their described smalls(t): Signature: Tree -> List of Trees
""Return the non-leaf nodes in t that are smaller than all their descendants.
       >>> a = Tree(1, [Tree(2, [Tree(4), Tree(5)]), Tree(3, [Tree(0, [Tree(6)])]))
>>> sorted([t_label for t in smalls(a)])
                                                                                                                                                                       2 🖾
                                                                                                                                                                                       0 🖾
                                 Signature: Tree -> number
): "Find smallest label in t & maybe add t to result"
       result = [] Sig

def process(t): "F:

    if t.is_leaf():

        return t.label

    else:
       return min(...)
process(t)
return result
```

**Designing Functions** 

Applying the Design Process

# Designing a Function

```
Implement smalls, which takes a Tree instance t containing integer labels. It returns the non-leaf nodes in t whose labels are smaller than any labels of their descendant nodes.
     non-tear nodes in t whose labels are smaller than any labels of their described smalls(t): Signature: Tree -> List of Trees
""Return the non-leaf nodes in t that are smaller than all their descendants.
          2 🔯
          return t.label
else:
smallest label; smallest = min([process(b) for b in t.branches])
in a branch of t if _rabbel < smallest
__rabbel < smallest
__result_append( t )
return min(smallest, t.label)
process(t)
return result
```

### Expression Trees

### Interpreter Analysis

How many times does scheme\_eval get called when evaluating the following expressions?

(define x  $(+|\hat{1}|\hat{2})$ )

(define (f y) (+ x y))

(f (if (>|3|2)|4|5))